

# Composition Dependence of Water Permeation Across Multicomponent Gel-Phase Bilayers

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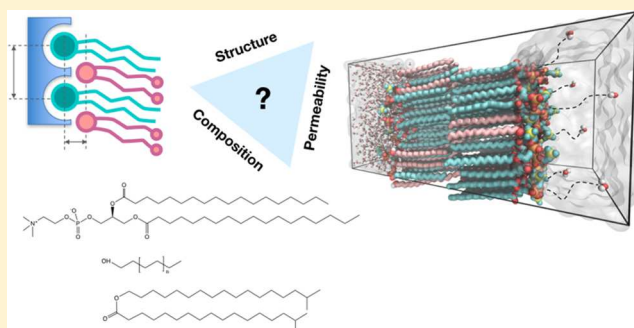
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## Supporting Information

**ABSTRACT:** The permeability of multicomponent phospholipid bilayers in the gel phase is investigated via molecular dynamics simulation. The physical role of the different molecules is probed by comparing multiple mixed-component bilayers containing distearylphosphatidylcholine (DSPC) with varying amounts of either the emollient isostearyl isostearate or long-chain alcohol (dodecanol, octadecanol, or tetracosanol) molecules. Permeability is found to depend on both the tail packing density and hydrogen bonding between lipid headgroups and water. Whereas the addition of emollient or alcohol molecules to a gel-phase DSPC bilayer can increase the tail packing density, it also disturbed the hydrogen-bonding network, which in turn can increase interfacial water dynamics. These phenomena have opposing effects on bilayer permeability, which is found to depend on the balance between enhanced tail packing and decreased hydrogen bonding.



## INTRODUCTION

Permeation is essential to the regulating function of biological systems, such as the bilayers found in cell membranes,<sup>1</sup> including the blood–brain barrier,<sup>2</sup> and the lamellar lipid structures found in the skin.<sup>3,4</sup> Whereas the permeability of fluidlike (i.e., liquid-crystalline) bilayers has been actively studied,<sup>5–8</sup> little work has focused on dense gel-phase mixtures, for which the permeability is likely to be dictated by different mechanisms than for fluidlike bilayers. For example, it has been suggested that the barrier domain is located deeper in fluidlike phospholipid bilayers than in gel-phase bilayers.<sup>9</sup> This is based upon the idea that for fluidlike bilayers the area occupied by the lipid tails exceeds the projected headgroup area and thus provides space for water molecules to be able to freely move between the lipid headgroups; in contrast, gel-phase systems tend to have densely packed headgroups, which limits the water mobility at the interface.<sup>10</sup> It is also known that the diffusion coefficient of water in a fluidlike bilayer interior is similar to that of bulk water,<sup>11</sup> whereas water diffusion in gel-phase bilayers is typically 2 orders of magnitude smaller than in bulk.<sup>12</sup> As such, although partitioning has been suggested to be the rate-limiting step in the permeability of fluidlike bilayers,<sup>11</sup> diffusion may play a more dominant role in gel-phase bilayers. Experimentally, it is not possible to determine direct cause-and-effect relationships because of the difficulty of inferring molecular-level details from experiments. For example, some

researchers have ascribed a low permeability in gel-phase ceramide-based multicomponent bilayers to a hexagonal-to-orthorhombic transition in the lateral lipid packing, driven by the presence of long-chain free fatty acids,<sup>13</sup> whereas others have attributed the low permeability to a long-periodicity lamellar phase.<sup>14</sup> The permeability of ceramide-based bilayers has been reported to decrease further when emollient molecules (such as the ones considered in this study) are added.<sup>15</sup> This decrease has again been associated with the long-periodicity phase by some,<sup>15</sup> whereas others found little change in the lamellar phase and suggested that the formation of emollient domains decreased the permeability,<sup>16</sup> with emollients serving as space-filler molecules.<sup>17</sup>

These questions surrounding the permeability mechanism of gel-phase systems clearly indicate that the process is not fully understood. Although various experimental methods are able to measure permeability, they are unable to elucidate local contributions to the membrane resistance or the pathway of the permeating molecules. Molecular dynamics (MD) simulations have played a key role in the study of bilayer permeability since the pivotal paper by Marrink and Berendsen in 1994,<sup>18</sup> in which MD was used to investigate the permeation

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of water across a fluidlike dipalmitoylphosphatidylcholine (DPPC) bilayer. The authors derived the inhomogeneous solubility–diffusion equation, which relates the bilayer permeability to the one-dimensional excess free energy and transverse diffusion coefficient profiles across the bilayer. It thus relates a global property, which can be compared to experiments, to local information that is not accessible in experiments, but available in a simulation. The number of simulations reporting permeability has increased rapidly in recent years,<sup>7,19,20</sup> with a particular focus on the permeation of small drug molecules across fluidlike bilayers.<sup>2,21–24</sup> Simulations of gel-phase bilayer permeability are far less common because of the high computational cost of gel-phase bilayer simulations combined with the cost of permeability simulations. Some studies<sup>25,26</sup> have mitigated these issues by calculating only free-energy profiles and not permeability; permeability also requires the determination of the diffusional contribution. Such an approach can give an indication of how different bilayers or permeants compare but is not sufficient to provide a detailed understanding of permeation mechanisms.

To the best of our knowledge, permeability coefficients for water in gel-phase bilayers have been calculated *in silico* by two groups;<sup>27–29</sup> however, neither of which considered gel-phase phospholipid bilayers or the effect of long-chain alcohols/emollients on bilayer permeability. In one study, Das et al.<sup>27</sup> calculated via MD simulations the permeation of water across ceramide-based lipid bilayers. The free-energy barrier was found to be twice that of a fluidlike phospholipid bilayer and was attributed to the denser tail packing in the gel phase. Furthermore, once water permeated past the lipid headgroups, it could diffuse easily through the tail region, such that the free energy of solvation was the main barrier to permeation. Others<sup>30</sup> have compared the permeation of small hydrophobic drug molecules through a fluidlike dioleoylphosphatidylcholine (DOPC) bilayer and through a gel-phase ceramide bilayer. The penetration free energy barrier was found to be larger and closer to the surface for the gel-phase ceramide bilayer, owing to its dense tail packing. Another MD study<sup>28</sup> focused on permeation of hydrophilic and hydrophobic molecules across gel-phase ceramide bilayers. Although the diffusion profiles obtained were qualitatively similar for each of the permeate molecules, the barrier domain was found to be located deeper into the bilayer interior for hydrophilic permeates than for hydrophobic ones. The same group subsequently studied the effect of ceramide tail length on the permeability of water and found that the permeability decreased with an increasing ceramide tail length.<sup>29</sup>

The aim of the present study is to explore the composition–structure–permeability relationships of gel-phase phospholipid-based bilayers. To this end, the permeability and structural properties of different pure and mixed-component bilayers are compared, with lipid molecules varying in tail length, headgroup chemistry, number of tails per molecule, and tail side branching. Specifically, we examine systems whose structural properties have been previously studied in detail,<sup>31,32</sup> namely, pure distearylphosphatidylcholine (DSPC) bilayers and binary mixtures of DSPC with isostearyl isostearate (ISIS, an emollient molecule) and with alcohol molecules with acyl tail lengths of 12 (lauryl or dodecanol), 18 (stearyl or octadecanol), and 24 (lignoceryl or tetracosanol) carbon atoms (see Table 1). The lauryl, stearyl, and lignoceryl alcohols are henceforth referred to as C12, C18, and C24, respectively. The remainder of this article is organized as follows. First, details of

Table 1. Overview of the Bilayers Simulated in This Study<sup>a</sup>

	pure	7:1	3:1	1:1	1:2
DSPC	✓				
DSPC–ISIS		✓		✓	
DSPC–C12		✓	✓	✓	✓
DSPC–C18				✓	
DSPC–C24				✓	

<sup>a</sup>Each system contains either pure DSPC or DSPC mixed with emollient (ISIS) or alcohol molecules with tail lengths of 12, 18, or 24 carbons in the compositions indicated.

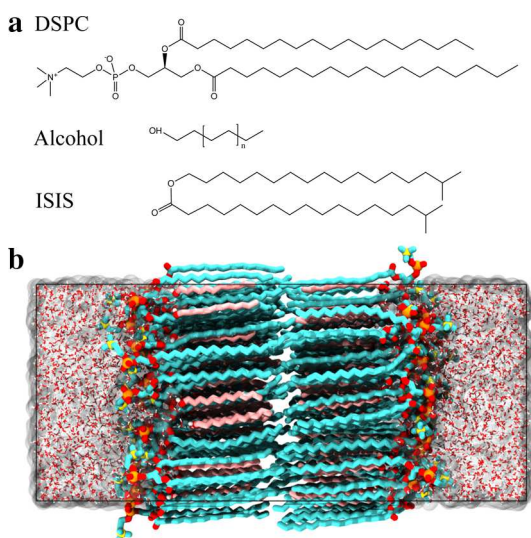
the simulations and analysis are given, followed by a discussion of bilayer permeability theory. We then present and discuss our results and, finally, summarize our findings and draw conclusions.

## MATERIALS AND METHODS

**Simulation System.** The structural properties and permeability of a pure DSPC bilayer and eight two-component DSPC-based bilayers were investigated, as listed in Table 1. Compositions were varied from bilayers in which the phospholipid concentration dominates (7:1) to systems in which the alcohol molecules dominate (1:2).

Bilayers were assembled by placing 2 leaflets, each with 64 lipids organized in a square lattice, in a bath of 2560 water molecules, where the initial lattice spacing was chosen to correspond to an area per lipid (APL) of approximately 20% larger than the estimated final APL, based on prior simulations.<sup>31,32</sup> This larger initial APL enabled lipids to rearrange and reorient during the equilibration. The lipids were initially randomly rotated about their long axis and tilted 10° with respect to the bilayer normal. The lipids in the two-component bilayers were randomly distributed among the lattice sites to mimic a mixed system, with both leaflets having a different random arrangement with the same relative lipid concentration. The importance of random rotations about the long axis of molecules was recently demonstrated for a phosphatidylethanolamine bilayer in the gel phase;<sup>33</sup> unrealistic tilt of the lipid tails has been observed if the lipid backbones (i.e., the part connecting the two tails of a molecule) are initially aligned in the bilayer plane. The headgroup of the alcohol or emollient molecules was placed at the same depth as the phosphate group of the phospholipids. Lipids were represented by the united atom GROMOS g53a6 forcefield<sup>34</sup> with partial charges from Chiu et al.<sup>35</sup> for the DSPC molecules, whereas the other molecules were created using Automated Topology Builder Version 2.1.<sup>36</sup> Water was modeled with the simple point charge (SPC) model, with the rigid structure preserved using the SHAKE algorithm. MD simulations were performed using the LAMMPS simulation engine.<sup>37</sup> Dispersion interactions were described by a Lennard-Jones potential, with a cutoff distance of 14 Å. The particle–particle–mesh method was used to calculate electrostatic interactions, with the real part truncated at 14 Å.<sup>38</sup> The Nosé–Hoover thermostat and barostat were used to maintain a constant temperature of 305 K and a pressure of 1 atm, respectively. Following the protocols that were used and validated in prior work to equilibrate the systems studied,<sup>31</sup> each bilayer was simulated for 160 ns, of which the last 60 ns was used for structural analysis. The final configuration of each simulation was then used as a starting configuration for the permeability simulations, as described below. Figure 1 provides the structures of the

molecules studied and a representative simulation snapshot for a (1:1) DSPC–C12 alcohol bilayer immersed in water.



**Figure 1.** (a) Structure of the DSPC, alcohol, and ISIS molecules. (b) Snapshot of a typical bilayer configuration of an equimolar mixture of DSPC and C12 alcohol immersed in water. Hydrocarbons are shown in cyan (DSPC) and pink (alcohol), oxygen is shown in red, phosphorus is shown in orange, nitrogen is shown in yellow, and hydrogen is shown in white.

The atom positions and the size of the simulation box throughout the simulation were used to calculate the area per lipid (APL), the offset distance, the bilayer height,  $H$ , the average tail tilt angle,  $\theta$ , and the area per tail (APT). The APL was calculated by dividing the cross-sectional area of the simulation box by the number of lipids in the leaflet. The offset distance was determined as the difference between the average depth ( $z$ -position) of the phosphate group of the DSPC molecules and the hydroxyl (alcohol) or ester (emollient) headgroup. The bilayer height was defined as the distance between the average  $z$ -position of the phosphates in both leaflets. The tilt of lipid tails was calculated from the average angle between the long axis of each tail and the transmembrane axis, where the long axis is the eigenvector corresponding to the minimum eigenvalue of the inertia tensor. Finally, the APT was calculated by dividing the APL by the average number of tails per molecule and multiplying this by the cosine of the average tilt angle, to project the area onto a plane perpendicular to the average chain direction. The APT can be considered as an inverse tail packing density, with the packing considered in the plane perpendicular to the orientation of the tails.

**Permeability Calculations.** The global permeability coefficient,  $P$ , can be calculated from the inhomogeneous solubility–diffusion equation<sup>18</sup>

$$\frac{1}{P} = R = \int_{-\infty}^{\infty} R(z) dz = \int_{-\infty}^{\infty} \frac{e^{\beta \Delta G(z)}}{D(z)} dz \quad (1)$$

where  $R$  is the resistance,  $\beta$  is the inverse of the thermal energy,  $\Delta G(z)$  is the local excess free energy, and  $D(z)$  is the local diffusion coefficient. We note that eq 1 can be derived from the one-dimensional Nernst–Planck equation assuming that the system is at a steady state.<sup>7</sup> Furthermore, the use of eq 1 is based on the assumption that the movement of a permeating molecule across the bilayer is the only relevant slow variable in

the system.<sup>39</sup> The diffusion coefficient and free energy were calculated via the  $z$ -constraint method,<sup>18</sup> which has been widely adopted because it simultaneously provides access to the excess free energy and the transverse diffusion coefficient profiles, in contrast to other methods, which can be used only to calculate either the free energy<sup>24,40,41</sup> or the diffusion coefficient profile.<sup>42–44</sup> In the  $z$ -constraint method, the excess free energy and diffusion profiles are calculated from the forces in the  $z$ -direction acting on “tracer” water molecules constrained in  $z$  along the transmembrane axis as

$$\Delta G(z) = - \int_{-\infty}^z \langle F_z(z') \rangle dz' \quad (2)$$

$$D(z) = (R_g T)^2 / \int_0^{\infty} \langle \Delta F_z(z, t) \Delta F_z(z, 0) \rangle_z dt \quad (3)$$

where the angular brackets denote an ensemble average,  $R_g$  is the gas constant,  $T$  is the temperature, and  $\Delta F_z = F_z - \langle F_z \rangle_t$  is the force fluctuation. Between 35 and 48  $z$ -positions (depending on the bilayer height; see Table S1 in the Supporting Information) were defined, separated by 2 Å. A randomly selected water molecule was moved to one of the  $z$ -positions (“windows”) and then constrained in  $z$  (additional details provided in the Supporting Information). The simulation system was then equilibrated for an additional 500 ps beyond the initial 160 ns, followed by a 1.3 ns simulation during which the net  $z$ -force on the constrained water molecule was measured. These relaxation and sampling times, although short compared to the slow lipid dynamics, are a multiple of the slowest relaxation time of water molecules in the bilayer. Specifically, the force autocorrelation functions indicate a maximum relaxation time of 200–300 ps in the headgroup region, where water molecules form hydrogen bonds (HBs) with their environment. Shorter relaxation times were found in the tail region where water molecules were observed to move through the triangular voids between the hexagonally packed tails, thus requiring no lipid reorganization and no hydrogen bonds to be broken or formed. Furthermore, no unconstrained water molecules were found to partition into the lipid tail region along with the tracer molecule. To sample a water molecule at various locations in the bilayer and to reduce statistical uncertainty, between 35 and 75 simulations (“sweeps”) were performed for each window, with different random water molecules selected from the aqueous phase. Sampling multiple locations is particularly important to accurately represent the lateral heterogeneity of multicomponent bilayers. The computational efficiency was improved by simultaneously sampling multiple water molecules in different windows that were separated by at least 1 nm in the  $z$ -direction (see Figure S1 in the Supporting Information). Sweeps were performed until the relative uncertainty in the free-energy profile was less than 5%; bilayers with a large energy barrier typically required more sweeps than bilayers with a small barrier. The uncertainties in the calculated diffusion and excess free energy profiles both contribute to a greater uncertainty in the resistance profile, which propagates further by integrating over the profile, resulting in a final uncertainty in the permeability coefficients of approximately 20%. Even though these uncertainties are considerable, they do not affect the comparison between bilayers because the difference between the permeability coefficients is found to be much larger. Additional details on the sampling process are given in the Supporting Information.

**Table 2. Overview of Structural Properties (Area per Lipid, Area per Tail, Offset, Bilayer Height, and Tilt Angle) for the Bilayers Studied<sup>a</sup>**

	APL [ $\text{\AA}^2$ ]	APT [ $\text{\AA}^2$ ]	offset [ $\text{\AA}$ ]	$H$ [ $\text{\AA}$ ]	$\theta$ [deg]
DSPC	50.1 (0.3)	20.2 (0.2)		48.2 (2.1)	36.4 (0.7)
(7:1) DSPC–ISIS	44.3 (0.2)	19.9 (0.1)	8.0 (0.7)	53.1 (2.1)	25.9 (1.4)
(1:1) DSPC–ISIS	42.5 (0.1)	20.1 (0.1)	6.6 (0.6)	54.8 (1.7)	18.8 (0.7)
(7:1) DSPC–C12	43.3 (0.1)	20.0 (0.1)	8.9 (0.6)	50.8 (1.8)	30.1 (0.2)
(3:1) DSPC–C12	37.5 (0.2)	20.0 (0.1)	8.6 (0.6)	53.6 (1.8)	21.1 (0.7)
(1:1) DSPC–C12	29.4 (0.1)	19.4 (0.1)	7.5 (1.0)	54.1 (1.8)	7.4 (0.4)
(1:2) DSPC–C12	26.1 (0.1)	19.5 (0.1)	6.9 (0.6)	52.0 (1.8)	6.1 (0.2)
(1:1) DSPC–C18	30.5 (0.1)	19.8 (0.1)	5.3 (0.5)	56.4 (1.4)	13.7 (0.4)
(1:1) DSPC–C24	30.0 (0.2)	19.6 (0.1)	5.8 (1.0)	63.0 (1.6)	10.8 (1.0)

<sup>a</sup>The numbers in parentheses are error estimates based on the standard deviation.

## RESULTS AND DISCUSSION

**Structural Properties.** In previous work,<sup>31,32</sup> the structure of a pure DSPC bilayer and equimolar mixtures of DSPC with alcohol or emollient molecules was investigated in detail. Although the systems in the present study are similar, smaller bilayers are considered (128 lipids instead of 200) to offset the large computational cost of permeability calculations. We first validated that the structural bilayer properties (listed in Table 2) are in good agreement with those calculated for the larger bilayer systems.<sup>31,32</sup> Specifically, the APL and tilt angle of the pure DSPC bilayer studied here are 50.1 (0.3) and 36.5 (0.7) $^\circ$   $\text{\AA}^2$ , respectively, compared to 49.7 (0.2) and 36.3 (0.4) $^\circ$   $\text{\AA}^2$  for the larger systems.<sup>31</sup> Even closer agreement is found for each of the equimolar multicomponent bilayers, indicating that size effects are negligible for the systems considered. This is consistent with the findings of Tjörnhammar and Edholm,<sup>45</sup> who simulated gel-phase phospholipid bilayers containing between 128 and 1296 lipids and found no significant system size dependence.

The headgroup size largely determines the APL of pure phospholipid bilayers in the gel phase because the projected headgroup area is larger than the combined cross-sectional area of the two acyl tails.<sup>9</sup> This mismatch between cross sections is compensated for by a collective tilt of the lipid tails with respect to the transmembrane axis, thus increasing the packing density of the tails. The APT found for the pure DSPC bilayer is 20.2  $\text{\AA}^2$ , in good agreement with the 19.8  $\text{\AA}^2$  found via X-ray diffraction.<sup>10</sup> Combining the lipids with molecules that have a smaller headgroup has two major effects on the bilayer structure. First, the presence of other molecules increases the distances between phosphatidylcholine (PC) headgroups and thus mitigates the steric effects of the PC headgroups.<sup>31</sup> Second, the difference between the molecular structures of the molecules facilitates a more efficient spatial packing and an offset forms between the headgroup depths in the bilayer.<sup>31</sup> The effects of these mechanisms on the APT vary with the concentration of the added molecule type, with large alcohol concentrations resulting in an APT as low as 19.4  $\text{\AA}^2$ . Although the offset between headgroup depths helps facilitate dense tail packing, the packing density does not always scale with the offset distance; increasing the alcohol or emollient concentration decreases the offset (owing to the decreased PC concentration), whereas it increases the packing density. Similar to the offset, the chain tilt is also closely related to the composition (i.e., the concentration of PC groups) because tilt is a consequence of the mismatch between the headgroup size and the cross section of the tails. The pure DSPC bilayer has the largest tilt (36.4 $^\circ$ ) of the bilayers considered, but the tilt

drops to 25.9–30.1 $^\circ$  when only 12.5 mol % of alcohol or emollient molecules is added to the bilayer (i.e., 7:1 mixtures), with the resulting tilt depending on the size and structure of the added molecule. The tilt angle of bilayers containing 50 mol % alcohol depends on the offset, which in turn depends on the relative tail lengths of the different molecules in the bilayer.<sup>32</sup> Tail-length asymmetry tends to increase the offset and leads to a smaller APL, APT, and tilt than in mixtures with symmetric tail lengths (i.e., DSPC–C18). Shorter alcohol molecules (C12) can sink further into the bilayer than longer ones (C24), as shown by the location of the alcohols in the bilayer density profiles (Figure S2, Supporting Information). A large concentration of short alcohol molecules thus results in the smallest tilt, around 6–7 $^\circ$ . Finally, the bilayer height does not follow a clear trend with the alcohol or emollient concentration.

**Water–Lipid Hydrogen Bonds.** It has been suggested that water partitioning into a bilayer depends on the affinity of lipid headgroups to form hydrogen bonds with water molecules.<sup>46</sup> Although this affinity is typically seen as a property of the molecule, our recent study of multicomponent gel-phase bilayers showed that the number of hydrogen bonds and their residence times depended not only on the lipid headgroups but also on their environment and thus on the bilayer composition.<sup>31</sup> The average number of hydrogen bonds per molecule and the hydrogen-bond residence times are calculated here (Table 3) to investigate the link among permeability, hydrogen bonding, and bilayer composition. The criterion used to determine the presence of a hydrogen bond was based on a combination of the O $\cdots$ H distance,  $r_{\text{OH}}$ , being

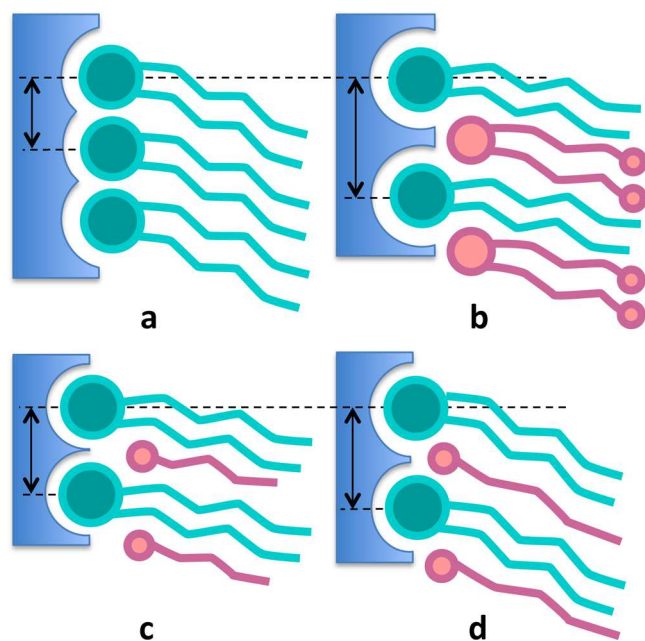
**Table 3. Number of Hydrogen Bonds between Water and a DSPC or an Alcohol/ISIS (A, I) Molecule in the Bilayer<sup>a</sup>**

	DSPC	A, I	HB/mol.	$\tau_{\text{DSPC}}$ [ps]	$\tau_{\text{AI}}$ [ps]
DSPC	3.29		3.29	192.3	
(7:1) DSPC–ISIS	3.58	0.40	3.19	119.1	145.0
(1:1) DSPC–ISIS	3.88	0.62	2.25	72.5	64.1
(7:1) DSPC–C12	3.44	0.43	3.06	111.6	327.3
(3:1) DSPC–C12	3.45	0.69	2.83	115.9	324.9
(1:1) DSPC–C12	3.85	0.74	2.30	80.4	191.6
(1:2) DSPC–C12	4.33	0.89	2.03	52.3	97.1
(1:1) DSPC–C18	3.78	0.75	2.27	78.7	96.8
(1:1) DSPC–C24	3.86	0.78	2.32	77.9	109.1

<sup>a</sup>HB/mol. denotes the average number of water–lipid hydrogen bonds per molecule in the bilayer and  $\tau_{\text{DSPC}}$  denotes the average residence time of the water–DSPC and  $\tau_{\text{AI}}$  denotes the water–alcohol/ISIS hydrogen bonds.

$<2.35 \text{ \AA}$  and the  $\text{O}_j\text{-O}_i\cdots\text{H}_i$  angle,  $\angle\text{OOH}$ , being  $<30^\circ$ , where molecule  $i$  is the donor molecule and  $j$  is the acceptor.<sup>47</sup>

The data in Table 3 show that the number of hydrogen bonds per DSPC and per alcohol (or ISIS) molecule increases with the concentration of alcohol (or ISIS) in the bilayer. Nevertheless, the overall number of hydrogen bonds between water and the bilayer decreases with an increasing alcohol (or ISIS) concentration, caused by differences in headgroup hydration, as shown in Figure 2. The small distance between



**Figure 2.** Schematic to illustrate how the amount of headgroup hydration (depicted in blue) and the space for water to move around the headgroups depends on the size and concentration of molecular species. Little space is available around headgroups in a pure DSPC bilayer (a), whereas space around the headgroups becomes accessible to water when ISIS molecules are present (b) or to a lesser extent when short (c) or long (d) alcohol molecules are added.

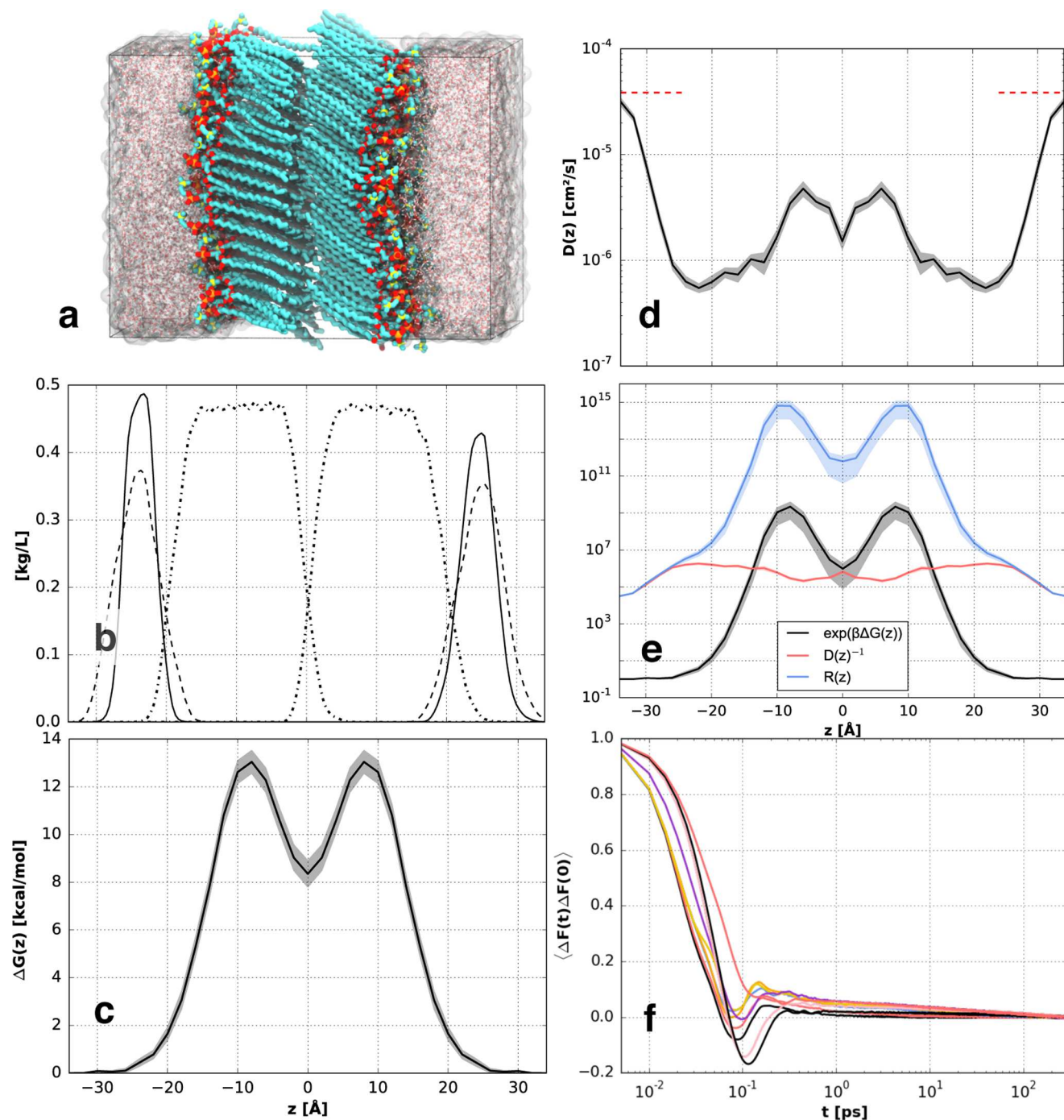
headgroups in a pure DSPC bilayer (Figure 2a) results in a partial hydration, such that the number of hydrogen bonds per PC headgroup is lower than that in a mixed-lipid bilayer, in which PC headgroups are further apart (Figure 2b–d). Similarly, an increase in the alcohol or ISIS concentration causes those headgroups to also become more accessible to water. Yet, the total number of hydrogen bonds per molecule decreases as more DSPC is replaced by alcohol or ISIS molecules because these molecules contain fewer potential hydrogen-bonding sites. Furthermore, the increased space between the headgroups gives rise to faster motion of the interfacial water, which results in shorter-lived hydrogen bonds compared to those seen in a pure DSPC bilayer. While the tail length of the alcohol molecules has a notable influence on the tail packing density and on the offset distance between headgroup depths, the tail length was found not to influence hydrogen bond numbers; however, the water–alcohol hydrogen-bond lifetime was found to increase with the depth of the alcohol headgroup in the bilayer.

**Permeability. Pure DSPC Bilayer.** The permeability of the pure DSPC bilayer (shown in Figure 3a) is first investigated to provide a baseline before the permeability of multicomponent bilayers is studied. Figure 3b–e shows the density, excess free

energy, diffusion coefficient, and resistance profile for the DSPC bilayer, respectively, whereas Figure 3f shows the force autocorrelation function corresponding to multiple windows ranging from the aqueous phase to the bilayer center. Time-averaged forces and force autocorrelation functions in each window were calculated for each sweep, after which the data were symmetrized about the middle of the bilayer and averaged over the sweeps to reduce the statistical uncertainty, depicted by the shaded areas in Figure 3c–e. The excess free energy ( $\Delta G(z)$ , Figure 3c) increases monotonically from 0, at the aqueous phase, toward its maximum of 13.1 kcal/mol, located in the dense tail region. The free-energy profile is comparable in shape and magnitude to the data presented by Das et al.<sup>27</sup> for a ceramide gel-phase bilayer. The free energy denotes the energetic cost of moving water from the aqueous phase to a certain depth into the bilayer, which is partially determined by the hydration energy. One of the important contributions to this energy is the cost of breaking hydrogen bonds; for example, the hydrogen-bond strength in bulk water is approximately 2.4 kcal/mol,<sup>48</sup> with each water molecule being involved in approximately 3.47 hydrogen bonds.<sup>47</sup> Thus, the combined hydrogen-bond energy of water is approximately 8.3 kcal/mol. Another contribution to the partition free energy involves the cost of placing a water molecule in a dense, unfavorable (hydrophobic) environment. The free energy decreases again toward the middle of the bilayer, where water molecules can escape the dense tail packing. Interestingly, the excess free energy in the middle of the bilayer is approximately equal to the hydrogen-bond energy of bulk water, suggesting that there is no significant cost to perturbing the bilayer when water is located between the two leaflets.

The transverse diffusion coefficient profile ( $D(z)$ , Figure 3d) decreases approximately 2 orders of magnitude from its bulk value, in the aqueous phase, toward a minimum value in the headgroup region, where water molecules are strongly confined and hydrogen-bonded to lipids and to other water molecules.<sup>31</sup> The diffusion coefficient then increases by an order of magnitude toward the tail region. This might seem counter-intuitive because diffusional freedom is often associated with available space. However, diffusion across the densely packed tail region in a gel-phase bilayer can more appropriately be seen as the movement of water toward a less unfavorable environment. Similarly, the diffusion coefficient in the middle of the bilayer is smaller, as it is unfavorable for water to diffuse from the middle into the denser tail region.

The resistance profile ( $R(z)$ , Figure 3e) across the bilayer is calculated from the partition coefficient profile,  $K(z) = \exp(\beta\Delta G(z))$ , and the inverse diffusion profile. The partition coefficient clearly dominates the shape of the resistance curve within the bilayer, whereas the resistance is diffusive outside of the bilayer. The local resistance varies over many orders of magnitude, such that the peak of the resistance profile predominantly determines the global resistance and permeability coefficient (calculated via eq 1). This demonstrates that the barrier domain is strongly heterogeneous, rendering, as expected, the classical “homogeneous” solubility–diffusion equation inadequate for bilayer permeability analysis.<sup>12</sup> Figure 3f shows the force autocorrelation function at various  $z$ -positions for the pure DSPC bilayer. Time integrals of these force autocorrelation functions are used to calculate the local diffusion coefficient. The correlation functions in the different windows show different decay behaviors depending on the local environments; the tail of the correlation function for the



**Figure 3.** (a) Simulation snapshot of a DSPC bilayer, (b) mass density profile of choline (dashed lines), phosphate/glycerol (solid lines), and the lipid tails (dash-dotted lines), (c) the excess free energy profile, and (d) diffusion profile corresponding to water permeating a gel-phase DSPC bilayer, with the reference bulk SPC water diffusion at 298 K<sup>49</sup> indicated by the red dashed lines, (e) resistance profile with the contributions due to free energy and diffusion, (f)  $z$ -force autocorrelation function for different windows ranging from the aqueous phase to the bilayer center. The shaded areas in (c)–(e) indicate the statistical uncertainty calculated from multiple sweeps.

window in the aqueous phase is shorter than 4 ps, which is similar to the rotational correlation time of bulk water.<sup>50</sup> Conversely, correlation times are 200–300 ps in the windows with the lowest diffusion coefficients (i.e., in the headgroup region), which are comparable to water–DSPC headgroups hydrogen-bonding lifetimes (192 ps, Table 3).

The simulated DSPC permeability is found to be  $P = 1.4 \times 10^{-8}$  cm/s, which is lower than the value  $P = 8.1 \times 10^{-7}$  cm/s measured via the  $\text{H}_2\text{O}/\text{D}_2\text{O}$  exchange method for DSPC at 293

K.<sup>46</sup> A similar discrepancy was reported by Das et al.,<sup>27</sup> who calculated the permeability of ceramide lipid membranes via MD simulations and found a value approximately 30 times smaller than that from the experiment. Conversely, Gupta et al.<sup>28</sup> computed the permeability of multiple permeants across a ceramide lipid bilayer and found a permeability coefficient for water that exceeded experimental results by almost 2 orders of magnitude. Similar discrepancies between experimental and computational permeabilities were found for fluidlike bilayers,<sup>51</sup>

but trends in the permeation simulations of different bilayers are found to be self-consistent and the MD simulations thus able to provide microscopic understanding and valid comparison between bilayers.

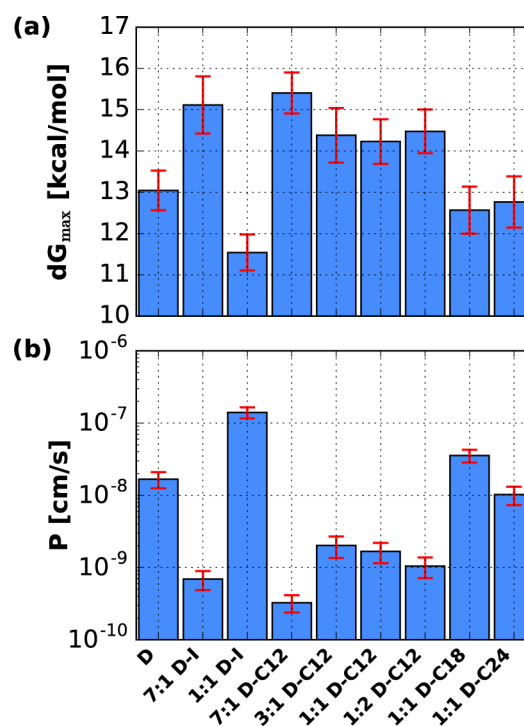
We consider here some factors that can contribute to inaccuracies in the simulated permeabilities. First is the simulation forcefield, which is optimized to model structural features of fluidlike bilayers.<sup>34</sup> Although the structural properties of gel-phase phospholipid bilayers are in good agreement with experiments, dynamics and interaction energies may be less accurate; this applies to the lipid forcefield as well as to water. The SPC model overestimates the experimental bulk diffusion coefficient of water at room temperature by 70%.<sup>49</sup> A second possible cause for deviation from experimental permeability values is the fact that the simulated bilayers do not show large defects, domain edges, or transient pores, which might be present in macroscopically large samples. In fact, recent X-ray measurements on gel-phase phospholipid bilayers have indicated the presence of low-frequency transverse modes associated with the formation of transient pores and lipid clusters.<sup>52</sup> Although the energetic cost of pore formation increases with the packing density of lipids,<sup>53</sup> pores could form in gel-phase bilayers but are not likely to be observed on the time and length scales accessible to MD simulation. Finally, the inhomogeneous solubility–diffusion equation is a simplified one-dimensional model that assumes homogeneity in the bilayer plane and transbilayer permeation to be the only slow variable. Such assumptions, although likely appropriate for small permeate molecules, such as water, are less suitable when large permeates are considered. Cardenas et al.<sup>39</sup> found, via MD simulation of tryptophan permeating a fluidlike DOPC bilayer, a permeability coefficient 32 times higher than in experiments when using the inhomogeneous solubility–diffusion equation and a rate twice the experimental value when using milestoning. The large discrepancy in the case of the inhomogeneous solubility–diffusion equation was due to deformation of the liquidlike bilayer caused by the large permeate molecules, whereas the milestoning approach was not affected by the deformation. We note that no bilayer deformation is observed in the present study, owing to the rigid gel-phase structure and the fact that the permeating water molecules are small.

In addition to the possibility of bilayer deformation, it was recently argued<sup>54</sup> that rotational motion should be taken into account when calculating the permeation of large molecules across a fluidlike bilayer; the same argument could potentially apply to small molecules permeating a densely packed gel-phase bilayer. However, in the present study, the permeating water molecules rotate to their preferred orientation within picoseconds, much faster than their translational motion, after which they do not rotate much. Force autocorrelation functions (Figure 3f) indicate that it takes up to 200–300 ps for forces to become uncorrelated, compared with approximately 4 ps in bulk water. In comparison, Marrink and Berendsen estimated a correlation time of 30 ps in the dense part of a fluidlike DPPC bilayer.<sup>55</sup> The fact that the correlation time is an order of magnitude longer in gel-phase bilayers than in fluidlike bilayers means that significantly more data are needed to obtain the same level of accuracy. Regardless, Das et al.<sup>27</sup> calculated force autocorrelation functions only up to 10 ps for gel-phase ceramide bilayers, with the length of the correlation function based on an estimated decay time in the ballistic regime. Such short correlation functions especially affect the regions where correlation times are long but also the reported bulk water

diffusion exceeded the diffusion coefficient associated with SPC water by 30%. Similar bulk diffusion values were found by Gupta et al., who did not report the length of the correlation functions.<sup>28</sup> Integrating the correlation functions up to 10 ps would lead to an overestimation of the diffusion in the tail region by approximately a factor of 4–5 based on our data.

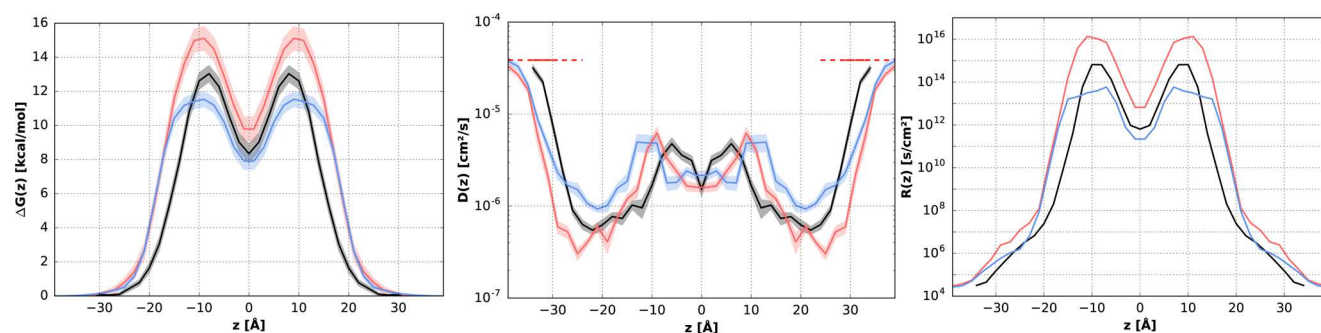
**DSPC–ISIS Bilayers.** Multiple experimental studies<sup>15,56</sup> have associated the presence of ISIS in ceramide-based gel-phase bilayers with a low permeability; however, these studies have not been able to determine the cause of the lower permeability. Nor have they investigated the range of conditions under which a decrease in permeability occurred. The influence of bilayer composition is of particular interest, as this can strongly affect structural properties, as discussed above. The bilayer permeability of the 7:1 and 1:1 DSPC–ISIS bilayers are compared here to investigate if composition has a strong influence on bilayer permeability.

The maximum free energy of the (7:1) DSPC–ISIS bilayer is found to be 16% larger than that of the pure DSPC bilayer, whereas the equimolar DSPC–ISIS mixture has a maximum free energy that is 13% lower than that of a pure DSPC bilayer (see Figures 4 and 5; peak values are provided in Table S2 in

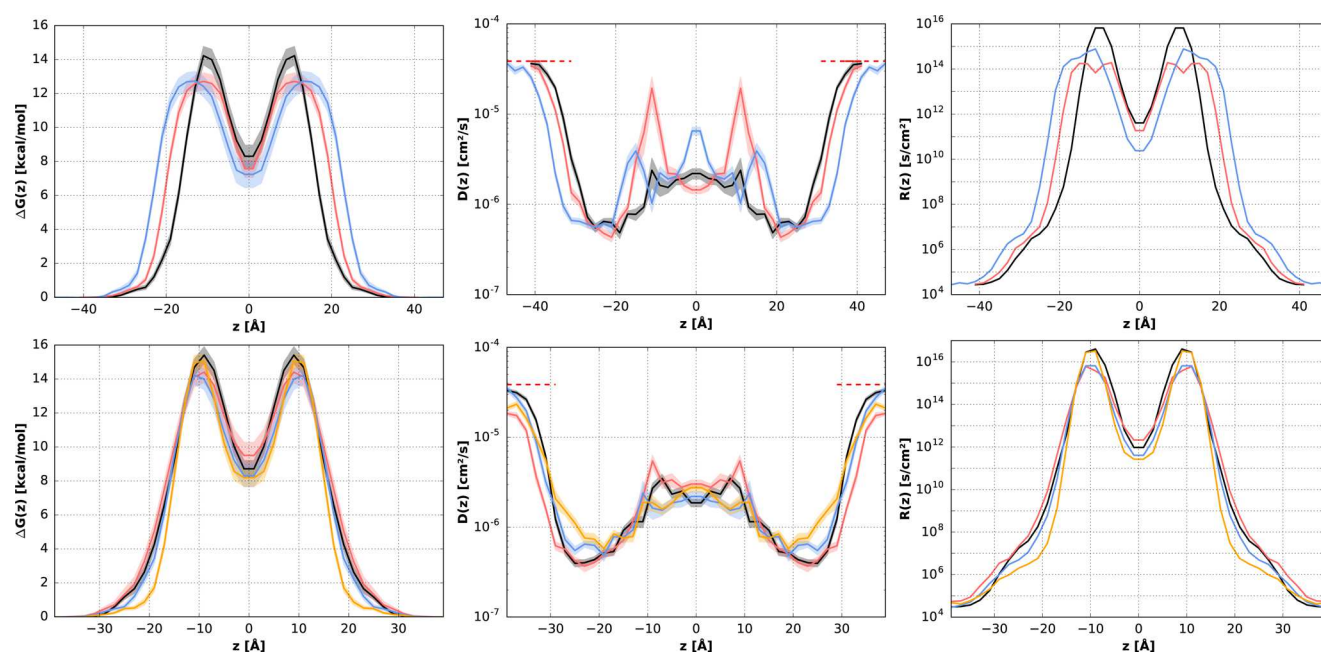


**Figure 4.** (a) Maximum free energy barriers and (b) permeability coefficient of the bilayers considered here. The uncertainty estimates are shown in red, with the uncertainty of the energy barrier calculated from the standard error of the sweeps and the permeability coefficients showing a propagated uncertainty.

the Supporting Information). The free-energy profiles in Figure 5 show that the equimolar DSPC–ISIS mixture exhibits less pronounced peaks in the tail region of the bilayer compared with those of the (7:1) DSPC–ISIS bilayer (mass density profiles corresponding to these bilayers are provided in Figure S2 in the Supporting Information). This is explained by the fact that the many side branches of the ISIS tails prevent dense packing (Table 2). The concentration of carbonyl groups, which are at the base of the DSPC tails, also decreases with an



**Figure 5.** Nonmonotonic influence of the ISIS composition in a DSPC bilayer on the excess free energy profiles (left), diffusion profiles (center), and resistance profiles (right). The profiles correspond to DSPC (black), 7:1 DSPC–ISIS (red), and 1:1 DSPC–ISIS (blue). The shaded area indicates the statistical uncertainty, calculated from the multiple sweeps.



**Figure 6.** Excess free energy profiles (left), diffusion profile (center), and resistance profile (right) of various bilayers. Top: The influence of the alcohol tail length. The profiles correspond to 1:1 DSPC–C12 (black), 1:1 DSPC–C18 (red), and 1:1 DSPC–C24 (blue). Bottom: The influence of the C12 alcohol concentration, with profiles corresponding to 7:1 (black), 3:1 (red), 1:1 (blue), and 1:2 (yellow) DSPC–C12 bilayers. The shaded area denotes the statistical uncertainty as calculated from multiple sweeps.

increasing ISIS concentration and in turn reduces hydrogen bonds between water and the carbonyl groups that decreases the diffusion coefficient in the tail region. Consequently, the diffusion in the equimolar mixture is larger than in the DSPC bilayer, whereas the diffusion coefficient in the (7:1) DSPC–ISIS bilayer is small due to the presence of many hydrogen bonds combined with a dense packing. The ISIS concentration clearly has a strong and nonmonotonic influence on the bilayer permeability. The lower permeability of the 7:1 mixture, compared to that of the pure DSPC bilayer and the equimolar DSPC–ISIS mixture, can be explained by its denser tail packing (Table 2), whereas the larger permeability of the equimolar DSPC–ISIS bilayer can be ascribed to differences between the headgroups of both molecule types. As shown in Table 3, the 1:1 DSPC–ISIS bilayer forms significantly fewer hydrogen bonds than the pure DSPC bilayer, and these hydrogen bonds are also shorter-lived, indicating faster water dynamics at the interface of the binary mixture. These few and short-lived hydrogen bonds, compared to those in the pure DSPC bilayer,

lead to a relatively high probability of water partitioning into the bilayer and thus a larger bilayer permeability.

In summary, the 7:1 DSPC–ISIS bilayer exhibits low permeability because of the combination of dense tail packing, significant hydrogen bonding, and slow dynamics in the headgroup region. The 1:1 DSPC–ISIS mixture has a tail packing density comparable to that of the pure DSPC bilayer, but the fewer and shorter-lived hydrogen bonds lead to a larger permeability.

**DSPC–Alcohol Bilayers.** The DSPC–alcohol bilayers are less permeable than bilayers containing ISIS at the same concentration, which is again caused by the differences in headgroup and a different lipid packing (Figure 2). Bilayers with alcohol molecules and those with ISIS form a similar number of hydrogen bonds with water (Table 3), but hydrogen bonds between water and alcohol molecules are more stable than those between water and ISIS, as evidenced by their longer residence time. This can be caused by the difference between the hydroxyl and the ester headgroup but also by the different available space for water molecules to move around, as depicted

in Figure 2. Because alcohol molecules have a single tail and no side branches on the tails, their projected area in the bilayer plane is smaller than that of the two-tailed ISIS molecules.

The DSPC–alcohol bilayers considered here show that the alcohol tail length affects the bilayer permeability, with the C12 mixtures having the smallest permeability coefficient, followed by the DSPC–C24 bilayer, whereas the DSPC–C18 bilayer is most permeable. This shows again that permeability does not scale with the bilayer height (i.e., tail length), as was suggested in the classical solubility–diffusion equation.<sup>12</sup> Such a scaling would also not be expected based on the heterogeneous nature of the bilayers. The data in Figure 6 shows that the free-energy profiles of the C18 and C24 bilayer systems are very similar, whereas the free-energy profile of the C12 bilayer has a more pronounced peak in the tail region (the corresponding mass density profiles are provided in Figure S2 of the Supporting Information). The same characteristics can be found in the shape of the resistance profiles. The difference in permeability of the equimolar DSPC–alcohol bilayers is thus not caused by the difference in bilayer height, or by differences between headgroups, because these are the same, as are the hydrogen-bonding statistics corresponding to these bilayers. Therefore, the relative permeabilities of these bilayers depend predominantly on differences between their packing densities and interdigitation of lipid tails caused by the differences in tail lengths. DSPC/alcohol binary mixtures can form a densely packed bilayer when the tail lengths are asymmetric and especially when the alcohol tails are shorter than the DSPC tails, as explained in a previous study.<sup>32</sup> Indeed, the permeability coefficients of the equimolar mixtures with alcohol molecules follow the same relative trend as the APTs of these bilayers.

The data in Figure 4 and in Table S2 show that the permeability of the DSPC–C12 bilayers is low for each of the compositions studied, but it is not directly obvious how the composition affects the permeability of these bilayers. The 7:1 DSPC–C12 bilayer has a similar APT as that of the pure DSPC bilayer, suggesting that the headgroup region may be responsible for the low permeability of the mixture. Because the alcohol molecules have only one tail, the space between protruding DSPC headgroups is smaller for the 7:1 DSPC–C12 bilayer than for the 7:1 DSPC–ISIS bilayer, as evinced by the smaller APL. The small space between the polar DSPC headgroups reduces the mobility of the interfacial water molecules, as shown by the long hydrogen-bond residence times and by the low diffusion coefficient in the headgroup region (Figure 6). Owing to the dense headgroup region combined with a low APT, the 7:1 DSPC–C12 bilayer has a large free-energy barrier and a permeability coefficient of  $P = 3.3 \times 10^{-10}$  cm/s, 50 times smaller than that of a pure DSPC bilayer. As the alcohol concentration increases, more space is available for the water molecules to move around between the PC headgroups and the number of potential hydrogen-bonding sites decreases. The barrier of the headgroup region thus decreases with an increasing alcohol concentration, whereas the barrier of the tail region may increase if the tail packing density increases, making it harder for water molecules to partition into and through the tail region. This transition in the barrier domain is apparent from the shape of the resistance profile in Figure 6; the 7:1 DSPC–C12 bilayer has a larger resistance in the headgroup region than that for the 1:2 mixture, whereas both bilayers have a similar maximum resistance. The tail packing density of the 3:1 DSPC–C12 bilayer is similar to that

of the 7:1 mixture but exhibits fewer hydrogen bonds with interfacial water molecules. Consequently, the permeability is larger than that for the 7:1 mixture but still smaller than that of a pure DSPC bilayer. The 1:1 and 1:2 DSPC–C12 bilayers exhibit fewer hydrogen bonds than the bilayers with less alcohol, and the residence times of the hydrogen bonds are shorter, especially for hydrogen bonds between water and alcohol molecules. The diffusion coefficient in the headgroup region of these bilayers is much larger than that for the 7:1 and 3:1 mixtures, as shown in Figure 6. Although the headgroup region of the 1:1 and 1:2 mixtures provides relatively little resistance, the tail packing density of these bilayers is very dense, resulting in a slightly lower permeability for these bilayers than for the 3:1 DSPC–C12 bilayer.

## CONCLUSIONS

Passive permeation of water through phospholipid-based gel-phase bilayers has been investigated via MD simulation. The bilayers considered included distearylphosphatidylcholine (DSPC), either pure or combined with the emollient isostearyl isostearate (ISIS) or with long-chain (lauryl, palmityl, lignoceryl) alcohol molecules. These molecules are relevant to various biological systems as well as in healthcare applications. In addition to comparing different molecule types and tail lengths, different bilayer compositions were also considered to gain a comprehensive understanding of the role of molecular structure and chemistry in bilayer permeability. Differences in permeability of the bilayers studied are explained on the basis of the packing density, the number of water–lipid hydrogen bonds, and the hydrogen-bond residence times.

The permeability of the mixed-component bilayers was found to vary significantly between different compositions, even when tail packing densities were similar. Bilayer composition was shown to affect hydrogen bonding between interfacial water molecules and the bilayer because of the different headgroup chemistry of the lipids, alcohol molecules, and emollients. The number of hydrogen bonds formed affects the free energy of partitioning, whereas the hydrogen-bond lifetime is related to local diffusivity. The lowest permeability coefficients were found for bilayers in which a small amount of alcohol or emollient molecules was added to a DSPC bilayer. The permeation barrier of these bilayers profited from a reasonably dense tail packing combined with a dense hydrophilic headgroup region with little room for water to move around. The headgroups in these bilayers formed many long-lived hydrogen bonds with interfacial water molecules. Adding more additive molecules to the phospholipid bilayer resulted in a denser packing of the tails, whereas the headgroups formed fewer and less stable hydrogen bonds.

In summary, the headgroup region strongly affects the permeability of gel-phase bilayers, in contrast to fluidlike bilayers, for which the hydrophobic tails largely determine the bilayer permeability. Adding alcohol or emollient molecules to a gel-phase DSPC bilayer increases the space between protruding DSPC headgroups, which increases the interfacial water diffusion and diminishes the hydrogen bonding between lipids and interfacial water molecules. This, in turn, reduces the free-energy barrier of the headgroup region, whereas the free-energy barrier in the tail region may increase because of a denser tail packing. The global bilayer permeability results from a balance between these competing effects.

## ■ ASSOCIATED CONTENT

### ■ Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.jpcc.8b00747.

Further details about the implementation of the permeability simulations including tabulated free-energy barriers and permeability coefficients and the mass density profile for each of the bilayers considered in this study (PDF)

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### Notes

The authors declare no competing financial interest.

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# The Composition-Dependence of Water Permeation Across Multicomponent Gel-Phase Bilayers

## SUPPORTING MATERIAL

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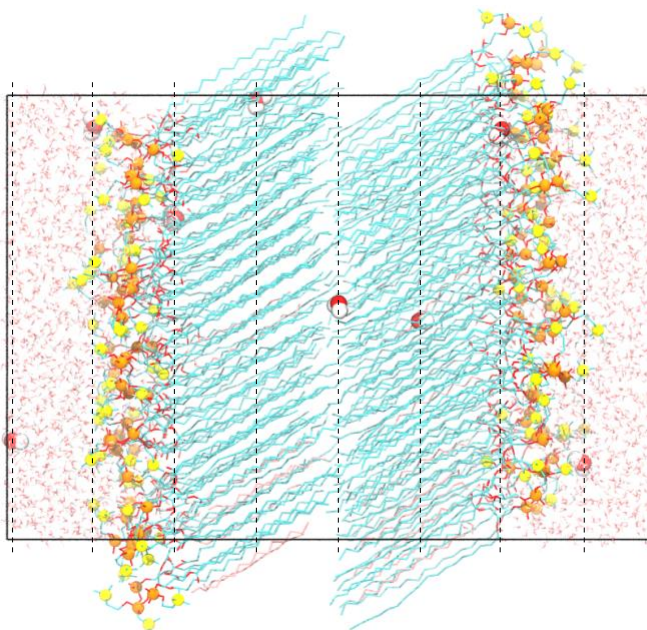
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### Implementation of the z-constraint method

Constraint forces on water molecules are calculated in windows separated by 2 Å. The number of windows is chosen to cover a range beyond the bilayer height, but smaller than the height of the simulation box. To account for the differences in bilayer height and box height, between 35 and 48 windows are used. Sampling in each window cannot be simultaneously performed, since strong interaction between water molecules in neighboring windows would affect the calculation. On the other hand, sampling only a single window per simulation is computationally inefficient. The total number of windows is chosen such that sampling of the windows can be evenly

distributed among 5 or 6 simulations. 7 or 8 windows are thus simultaneously sampled in each simulation, with the sampled windows separated in  $z$  by 1 or 1.2 Å (i.e., 5 or 6 windows apart, respectively). Figure S1 shows a snapshot of a (7:1) DSPC-C12 bilayer with 8 tracer molecules.



**Figure S1:** A (7:1) DSPC-C12 bilayer with 8 constrained water molecules at different  $z$ -positions.

The permeability simulations were initialized by first randomly selecting 7 or 8 tracer molecules from the aqueous phase. The center of mass of each of these tracer molecules was then connected to a weak harmonic spring ( $2.8 \times 10^6$  N/m) with the other end of the spring at a  $z$ -position corresponding to a window. These tracer molecules were free to move in  $x$  and  $y$ . After 20 ps the weak spring was replaced by a stronger spring ( $3.5 \times 10^7$  N/m) and the simulation was continued for an additional 20 ps to ensure that the tracer molecules are close to their corresponding window position. The spring was then removed and the  $z$ -position of the tracer molecule fixed at the  $z$ -position of the window, after which the system was equilibrated for 500 ps. The resulting configuration (Figure S1) served as the starting point for the first of the 5 or 6 permeability simulations needed to sample all windows. The starting configurations for the other simulations were created by moving each of the tracer molecules simultaneously at a constant

speed of 10 m/s in the  $z$ -direction and storing the configuration after each 20 ps (i.e., 2 Å). These configurations were again equilibrated for 500 ps.

Data was collected for 1.3 ns after equilibration. This sampling time is short compared to the slow motion of the lipids, but it is longer than the relaxation time of the water molecules in the headgroup region (where the smallest diffusion coefficients for water are observed), which is similar to the hydrogen bonding life time (up to 300 ps). Additional data is collected by repeating the sampling multiple times, with water molecules at different lateral positions in the bilayer. The repeated sampling of each window is referred to by ‘sweeps’, which were at least 35 (for more permeable bilayers) and maximum 75 (for most the most occlusive bilayer). Sweeps were performed until the maximum relative uncertainty in the excess free energy reached below 5%. The total amount of sampling per window is thus between 46 ns (i.e., 35 times 1.3 ns) and 98 ns. We note that Das *et al.*,<sup>1</sup> followed the same approach, but performed 15 sweeps and used a sampling time of 2 ns, thus effectively sampling each window for 30 ns. Table S1 shows an overview of the bilayer heights, number of windows, number of tracers, number of parallel simulations needed to complete a single sweep, and the number of sweeps performed for each of the bilayers considered.

### Additional data

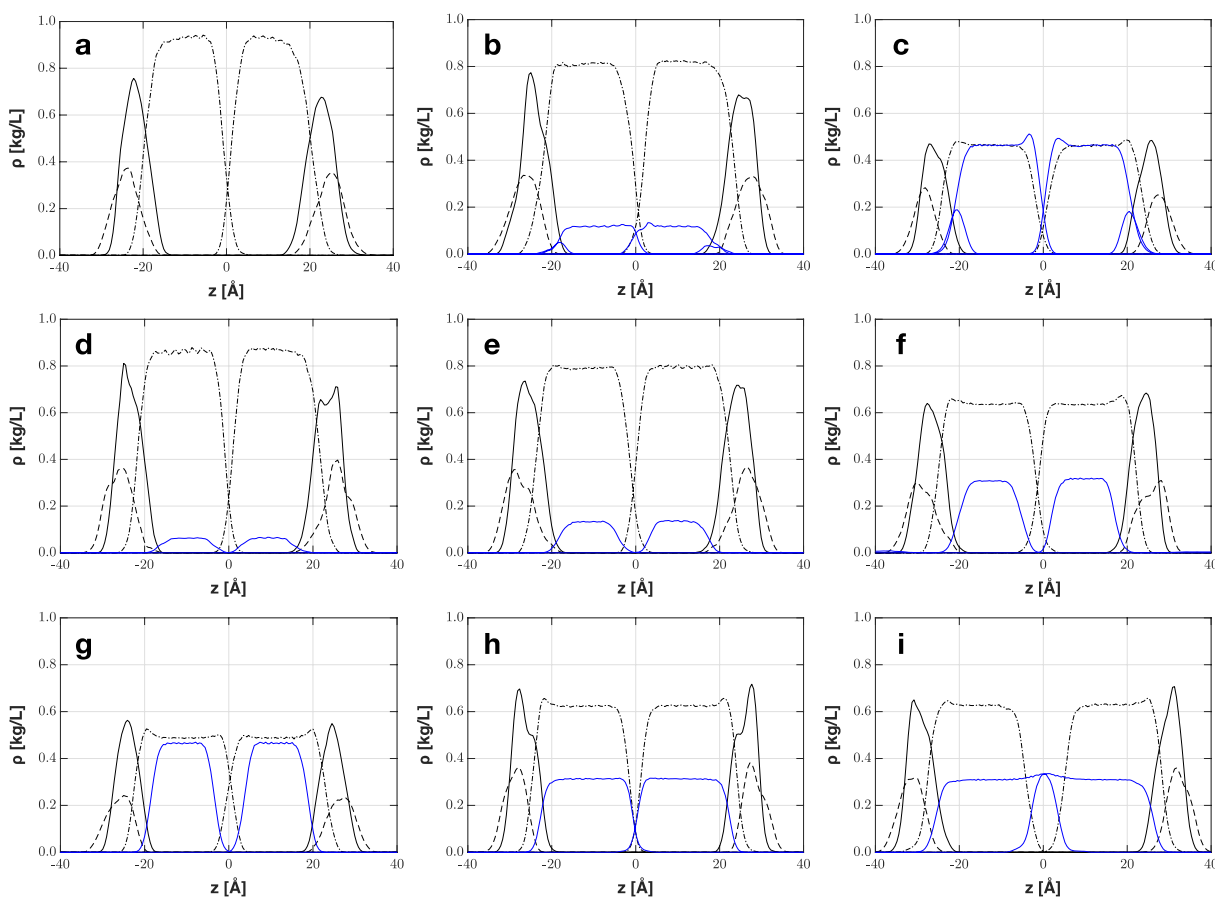
**Table S1:** Summary of the permeability simulations. Reported are the bilayer height  $\text{\AA}$ , the number of windows (each 2  $\text{\AA}$  wide), the number of simulations per sweep, and the number of tracer molecules per simulation. The numbers in parentheses are the standard deviation.

	H [ $\text{\AA}$ ]	Windows	Sim / sweep	Tracers	Sweeps
<b>DSPC</b>	48.2 (2.1)	35	5	7	50
<b>(7:1) DSPC-ISIS</b>	53.1 (2.1)	40	5	8	40
<b>(1:1) DSPC-ISIS</b>	54.8 (1.7)	40	5	8	40
<b>(7:1) DSPC-C12</b>	50.8 (1.8)	40	5	8	75
<b>(3:1) DSPC-C12</b>	53.7 (1.8)	40	5	8	35
<b>(1:1) DSPC-C12</b>	54.1 (1.8)	42	6	7	40
<b>(1:2) DSPC-C12</b>	52.0 (1.8)	40	5	8	35
<b>(1:1) DSPC-C18</b>	56.4 (1.4)	42	6	7	35
<b>(1:1) DSPC-C24</b>	63.0 (1.6)	48	6	8	35

**Table S2:** Summary of the excess free energy barrier and permeability coefficient for each of the bilayers studied. The numbers in parentheses are the standard deviation.

	$\Delta G(z)$ [kJ/mol]	P [cm/s]
<b>DSPC</b>	13.1 (0.5)	1.4e-8 (3.6e-9)
<b>(7:1) DSPC-ISIS</b>	15.1 (0.7)	8.2e-10 (2.5e-10)
<b>(1:1) DSPC-ISIS</b>	11.5 (0.4)	1.4e-7 (2.4e-8)
<b>(7:1) DSPC-C12</b>	15.4 (0.5)	3.3e-10 (8.7e-11)
<b>(3:1) DSPC-C12</b>	14.4 (0.8)	1.9e-9 (6.8e-10)
<b>(1:1) DSPC-C12</b>	14.2 (0.5)	1.7e-9 (5.2e-10)
<b>(1:2) DSPC-C12</b>	14.5 (0.6)	1.0e-9 (2.6e-10)
<b>(1:1) DSPC-C18</b>	12.7 (0.6)	3.1e-8 (6.3e-9)
<b>(1:1) DSPC-C24</b>	12.8 (0.6)	1.0e-8 (2.9e-9)

## Mass density profiles



**Figure S2:** Mass density profiles of (a) pure DSPC, (b) 7:1 DSPC-ISIS, (c) 1:1 DPSC-ISIS, (d) 7:1 DSPC-C12, (e) 3:1 DSPC-C12, (f) 1:1 DSPC-C12, (g) 1:2 DSPC-C12, (h) 1:1 DSCP-C18, and (i) 1:1 DSPC-C24. The DSPC density is shown in black, with choline in dashed lines, phosphate/glycerol in solid lines, and tails in dash-dotted lines. The blue lines represent the alcohol or ISIS molecules, with the ISIS ester headgroup and tails drawn separately.

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